

MDIA3008

∍ggi YgʻUbXʻ7 f]g]gʻ7 ca a i b]WUh]cb

GYa YghYf'C bY''##'&\$%

7ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
7 c``]b '7 \i U	Ü	HiYgXUmž-" \$Ua'hc %%" \$UažcfVm Uddc]bhaYbh	KYVghYf`&'%?	- ' ,)) - , ,

"Hi hcfg"

B Ua Y	9a U]`	5j U]`UV]`]m	@cWUh]cb	D\cbY
DYhYf'F cVYfhg	d"^fcVYfhg4 i bgk "YXi "Ui			
GUa YYfU [.] 8i ffUb]	gUa YYfU"Xi ffUb]4 i bgk "YXi "Ui			
>UbY ->cfXUb	べたfXUb4 i bgk "YXi "Ui			
5XUa GHUd`Yhcb	U"ghJd`Yhcb4 i bgk "YXi "Ui			
B]X]U'FUmU'AUfh]bYn	b"fUmUa Uff¶bYn4 i bgk "YXi "Ui			

GWkcc~7cbhJWh~abZcfa Uhlcb

Fcca " %&ž"Yj Y" FcVYfhK YVqhYf'6i]X]b[

D\cbY. f\$&Ł'-',) '(,) *

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.##qUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[hcb'WJadig\cong \cong m1]U'`fP]hmUbX'5fti/'8Yg][b'7UadigYg\cong \cong m5W_bck`YX[Y'h\Y'B[ibbUk']Ub'\cong m2]b'7UbVYffU\cong m3b'7UbVYffU\cong m3b'7UbVYffU\cong m3b'7UbVYffU\cong m3b'7UbYYffU\cong m3b'7UbYffU\cong m3b'7$

5 hyb XUb WY F Yei]fYa Ybhg

5 'ghi XYbh']g'Yl dYWYX'hc'UhrYbX'U```WUgg'WcbhUWi\ci fg'Zcf'U'ZUWY!hc!ZUWY'fl &: Ł'cf'V`YbXYX'Wci fgY'UbX Wca d`YhY'U```UWYj]h']Yg'Zcf'U'VYbXYX'cf'Z ``mcb`]bY'Wci fgY"

5 'ghi XYbhik \c'Uff]j Yg'a cfY'h\Ub'%) 'a]bi hYg'``UhY'a Um'VY'dYbU`]gYX'Zcf'bcb!UhhYbXUbWY'''=Zgi W\'U'dYbU`hm]g']a dcgYXž'h\Y'ghi XYbha i gh'VY']bZcfa YX'j YfVU``mUh'h\Y'YbX'cZWUgg'UbX'UXj]gYX']b'k f]h]b['k]h\]b'&(\ci fg"

⊒Uʻgh XYbhYl dYf]YbWrgʻ]`bYggža]gUXj Ybh fYʻcfʻch\YfʻcWW ffYbWrʻh\Uha U_YgʻUVgYbWʻZfca ʻU WUgg#UWfj]hmi bUj c]XUV`YžcfʻYl dYWgʻhcʻVYʻUVgYbhZfca ʻUʻZcfh\Wca]b[ˈWUgg#UWfj]hmžh\Ymg\ci `XʻgYY_ dYfa]gg]cbʻZfca ʻh\Yʻ7 ci fgYʻ5i h\cf]hmžʻUbXʻk \YfYʻUdd`]WUV`Yžh\Y]fʻfYei Yghg\ci `XʻVYʻUVWca dUb]YXʻVmUb cf][]bUʻcfʻWYfh]ZYX`WcdmcZUʻa YX]WU`WYfh]ZWUhYʻcfʻch\YfʻZcfa `cZUddfcdf]UhYʻYj]XYbWY"

 $5.7 \text{ ci fgY} \cdot 5 \text{ i h} \cdot \text{cf} \text{lma UmYl W gY} \cdot \text{U} \cdot \text{ghi XYbh} \text{Z} \cdot \text{ca} \cdot \text{WUggYg} \cdot \text{cf} \cdot \text{UWhj} \text{ lh} \text{Yg} \cdot \text{Zcf} \cdot \text{i d} \cdot \text{hc} \cdot \text{cbY} \cdot \text{a cbh} \cdot \text{``} < \text{ck Yj Yf} \cdot \text{hh} \cdot \text{Ym}$ a $\text{UmUgg} \cdot \text{[hc]} \cdot \text{hc} \cdot \text{[hc]} \cdot$

7 ci fgY 8 YHJ]`g 7 fYX]hDc]bhg * Gi a a UfmcZh\Y 7 ci fgY

5ggYgga Ybh

 $H\ [g`57C5`XcW\ a\ Ybh']g`]bhYbXYX`df]a\ Uf]`mUg`U`dc`]WmXcW\ a\ Ybh'!\ d`YUgY`fYZYf`hc`h\Y`7ca\ dfY\Ybg]j\ Y`7ci\ fgY';\ i\]XY`gYWh]cb`cb`h\Y`AccX`Y`g]hY`Zcf`Wca\ d`YhY`]bZcfa\ Uh]cb`cb`h\Y`Wci\ fgY''$

5ggYgga Ybh'HUg_g'

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UhY	Gh XYbh@YUfb]b[CihWca Yg 5ggYggYX
G\cfh9ggUm	&) ।	' \$#\$' #&\$% `\$(.\$\$`DA	% <u>ž</u> (ž)
DfYgYbfUf]cb	&) ı	Bch5dd`]WUV`Y	%ž&ž(ž)
7 f]h]WU``5bU`mg]g'CF '7 f]g]g 7 ca a i b]WUh]cb'D`Ub') \$1	\$%#\$*#&\$% `%%) - `DA	%ž&Ž Ž(Ž)

5ggYgga Ybh'8YHJ]`g

5ggYgga Ybh% G\cfh9ggUm

GhUfh XUhY.

@Yb[h\. *\\$\$\$!\%) \$\$ k cfXg

 $\textbf{8YHJ} \texttt{`g.'K} \texttt{ cfX''Yb[h\.'\%\$\$!\%) \$\$'k cfXg'''H\]g'UggYgga Ybh]g']bhYbXYX'hc'hYghimci f'XYj Y`cd]b[$

Mci 'UfY'UXj]gYX'hc 'gY'YWhmci f'ei Ygh]cb'k]h\ 'WUfYž'Ug'h\ YmdcgY'X]ZZYfYbh'W\U``Yb[Yg'': cf']bghUbWfž ei Ygh]cb'cbY']g'ei]hY'[YbYfU`'-'hc'Xc'k Y``ž'mci f'W\U``Yb[Y'k]```VY'hc'VY'hc'dfcj]XY'U'f][cfci g'UbX YZYWf]j Y`mgi ddcfhYX'fUh]cbU'Yž'[efW\$V'cZg]a d`mdfcj]X]b['U'gYhcZVfcUX'UbX'[YbYfU`]gYX'gHUHYa Ybhg'' K]h\ 'ei Ygh]cbg'hk c'UbX'h\ fYYž'mci f'W\U``Yb[Y'k]```VY'hc'g\ck 'h\ Uhmci 'UfY'XYj Y`cd]b['U'gHfcb['cj YfU`` i bXYfghUbX]b['cZ]ggi Yg'UbX#cf'Wf]g]g'Wca a i b]WUh]cbž'[efW\$V'cZg]a d`mdfcj]X]b['U'bUffck 'fYgdcbgY XfUk b'Zca 'A ghcbY'k YY_'g'k cfh\ 'cZfYUX]b["

5ggYgga Ybh7f]hYf]U.

Mci 'Ufy'UXj]gYX'hc'Zc``ck 'h\]g'[YbYfU``Zcfa Uhk]h\'mci f'DfygYbhUh]cb"

- %" **±bffcXi Wh]cb**"K \UhUfY'mci 'hU`_]b['UVci h3'K \mi]g'h\]g'hcd]WfY`Yj Ubhff]"Y"žk \mig\ci `X'dYcd`Y WUfYŁ3'<ck 'UfY'mci 'hU\<u>'</u>]b['h\Y'hcd]Wfk \Uh]g'mci f'UddfcUW\'UbX#cf'a Yh\cXc`c[mŁ3
- &" Cj Yfj]Yk "'K \Uh'UfY'h\Y'_Ym'WcbhYl hg3'K \Uh'UfY'h\Y'a cgh']a dcfhUbh'XYj Y`cda Ybhg3'K \]W\'UfY h\Y'_Ym'UgdYWhg'cZh\Y']ggi Yg#Wf]g]g3
- " 5 bU`mg]g#fYWca a YbXUh]cbg" K \UhiUfY h\Y`_Yma]ghJ_Yg`UbX#cf`_Ymgi WW`ggYg`k]h\`fY[UfXg`hc Wca a i b]WUh]cbg`ghfUhY[m8`K < Mf\ck `WUb`mci `gi VghUbh]UhY`cf`gi ddcfhimci f`UbU`mg]g\2\K \Uh k ci `X`mci `fYWca a YbX3`K \UhiUfY`mci f`]bg][\hg3`< ck `WUb`mci `gi ddcfhimci f`dc]bhg`k]h\`fY`Yj Ubh ZJWgz`XUhJz`UbX#cf`h\YcfYh]WJ``ZfUa Yk cf_g3
- ("7cbWig]cb"K\UhUfY'h\Y'_YmhU_YUkUmg'mci k]g\'hc''YUjY'mcif'UiX]YbWY'k]h\3

K cf_]b[']b'U'ga U```[fci d'k]``'hmd]\WU``m\Y'U'\\cappa a cb'U\\f\j]\m\Zcf'k cf_]b[']b'h\Y']bXi ghfm''5'_YmdfYa]gY\\\]bX'h\]g'UggYgga YbhhUg_']g'Zcf'mci 'hc'hfYUhih\Y'\\cappa a ch'U\\f\j]hj\Yg'UbX'i b\\f\tau'f\U]bhj\Yg'cZ[fci d'XmbUa]\\g'UbX\]bh\YfU\\f\j bg'UgYga Ybh\Ug'U\J\\\]b\\f\Ub'\UgdY\\f\cZh\Y'`YUfb]b['dfc\\f\gg'-'Ug'U'j U'i UV'Y'cddcfhi b]\mcZdfU\\f\\\f\\\ Ub\X'\\cappa a]b['hc'h\Yfa g'k]h\'Ub'U\\f\j |\min\Unmci 'k]``bYYX'hc'\Y\\cappa a Y'dfc\Z\\Ybhk]\\"

5ggYgga Ybh7f]hYf]U.

- 5V]`]hmhc`k cf_'dfcZYgg]cbU``mUg`U`hYUa 'hc`hU_Y`W\Uf[Y`UbX'hc``YUX'U`DfYgYbhUh]cb"
- 5V]]|milic 'gY`YWhUbX'XYj Y`cd'Ub'Uddfcdf]UhY'WUgY'gh Xmž'k]h\ 'gWcdY'Zcf'UbU`mg]g"
- 5V]`]lmihc`Wc\YfYbhmUbX`dYfgi Ug]j Y`mWca a i b]WUhY`_Ym]XYUg`UbX`dc]bhg"
- 5V]`]hmhc`dfcj]XY`Ub`YZZYWf]j Y`UbX`gi WW]bWhcj Yf]]Yk ž`g\ck]b[`ghfcb[`i bXYfghUbX]b[`cZh\Y fY`Yj Ubh]bXi ghfmWcbhYl hg`UbX`]gqi Yg`fY`Uh]b[`hc`h\Y`gY`YWhYX`WUgY`ghi Xm"
- 5V]`]mihc`dfcj]XY`a YUb]b[Z``]bg][\hgž'UbU`mg]gž'UbX#cf`fYWca a YbXUh]cbgž'dfcdYf`migi ddcfhYX`Vm fY`Yj Ubh'WcbW'dhgž'XUhUž'UbX'h\Ycfm'
- 5V]`]lmihc`fYgdcbX'WYUf`mUbX'YZZYWf]j Y`mik \Yb'WkU``Yb[YX'k]h\'ei Ygh]cbg"

Gi Va]qq]cb bchYq. DfYqYbhUhcb cb m/bc Hi fb]hb qi Va]qq]cb fYei]fYX"

Hi fb]hb gYhb[. H\]g]g bchU Hi fb]hb Ugg][ba Ybh

5ggYgga Ybh' . 7f]h]WU` 5bU`mg]g CF 7f]g]g 7ca a i b]WUh]cb D`Ub

GHJfh:XUhY.

@Yb[h.77f]h]WU`5bU`mg]g`f&ž) \$\$!' \$\$\$`k cfXgtZ`CF`7f]g]g`7 ca a i b]WUh]cb`D`Ub`Ug`U`Wc``UVcfUh]j Y`dU]f fl ž) \$\$!(\$\$\$`k cfXgt"

8YHJ]`g. 'H\YfY`UfY`lk c`W.c]WYg`Uj U]`UV`Y`]b`hYfa g`cZh\]g`a U^cf`dfc`YWf`Mci `WUb`gi Va]h`Ub`]bX]j]Xi U` 7f]h]WU``5bU`mg]g`f&z) \$\$!' \$\$\$`k cfXgŁz`CF `gi Va]h`U`7f]g]g`7 ca a i b]WUh]cb`D`Ub`Ug`U`Wc``UVcfUhj Y`dU]f fl z) \$\$!(\$\$\$`k cfXgŁ"`H\]g`]g`h\Y`Z]bU``UggYgga Ybh'hUg_"K f]hhYb`ZYYXVUW_z`]b`Wcb^bbW]cb`k]h\`U`a Uf_]b[hYa d`UhY"

5XX]h]cbU`XYhJ]`g.

H\]gʻa UʻcʻfʻUggYgga Ybhik]```VYʻk cfh\`Uʻgi VgHJbhJU``dYfWYbhJ[YʻcZmci fʻZ]bU``a Uf_"'=i\UgʻVYYb`XY`]VYfUhY`m XYg][bYX'h\]gʻk UmžʻUgʻk cf_]b[i]bʻh\Y`]bXi ghfmik]``VY`XYdYbXYbhicbʻh\Yʻgi WWYggʻcZa Uʻcʻfʻdfc YWygʻmci iUfY]bj c`j YX'k]h\"`Gca YʻhJa Y`k]``VYʻgYhUg]XY`]b`WUggYgʻ`UhY`]bʻh\Y`gYa YghYfž`]b`cfXYfʻhc`k cf_g\cdʻh\Y`a Uʻcf UggYgga Ybh'

 $H\YfY`UfY`lk\ c`Wkc]W'g`Uj\ U]`UV`Y`]b`hYfa\ g`cZh\]g`a\ U^cf`dfc^Y\W''\Mci``WUb`gi\ Va\]h`Ub`]bX]j\]Xi\ U``7f]h]WU`5bU`mg]g`f&z)$$!'\$$$'k\ cfXgŁz'CF`gi\ Va\]h`U`7f]g]g`7ca\ a\ i\ b]WUh]cb`D`Ub`Ug`U`Wc``UVcfUh]j\ Y`dU]ff fl\ z)$$!($$$'k\ cfXgŁ''$

cfihly 7 fjhjwl 5 bu'mg]gžmci fihlg_jg'hc'Ubu'mgY'CB9'WugY'ghi Xm'i 5 gY'YWljcb'cZh\fYY'dcgg]V'Y'WugY ghi X]Yg'hc'WkccgY'Zfca 'k]``VY'dcghYX'cb'A ccX'Y'Uddfcl]a UhY'mik c'k YY_g'VYZcfY'h\Y'UggYgga Ybh XYUX']bY"'H\]g']g']bhYbXYX'hc'dfcj]XY'gca Y'gYa V'UbWY'cZh\Y'hJa Y'dfYggi fYžgdcbhUbY]lmž'UbX'`UW_cZZcfYg][\hih\UhdfcdYf'miWkUfUWhYf]gY'Wf]gYg'UbX']ggi Yg"'FZWeWUSeWefgV[We'i [^TWVcSi ` Xta_ SUfgS^ WhW feł S`Vi [^ZShWaUUgcbWi i [fZ[fZWbSef XhWkWScb"'7 UgY'ghi X]Yg'k]``VY'X]gWi ggYX']b''YWhi fYg h\fci [\ci hih\Y'gYa YghYf"

5 'gi [[YghYX'Zcfa Uh']g'Ug'Zc``ck g.

H\]g`Wca dUbm#cf[Ub]gUf]cb`WJb`VY`\mdch\Yf]WJ``cf`UWi U``'`=Zmci `W\ccgY`Ub`UWi U``Wca dUbm#cf[Ub]gUf]cbz mci `k]``bYYX`fc`UffUW\`U`g][bYX``YffYf`Zfca `U`Wca dUbmfYdfYgYbfUf]j Y`\c`X]b[`U`gYb]cf`a UbU[Ya Ybh dcg]f]cbz`WcbZ]fa]b[`fh\Uh`ff%"E'H\YmUfY`[]j]b[`mci `dYfa]gg]cb`fc`WfYUfY`U`7 f]g]g`7 ca a g`D`Ub`Zcf`fh\Y Wca dUbm#cf[Ub]gUf]cb`XcYg`bch\Uj Y`U'dfY!Yl]gf]b[`7 f]g]g`7 ca a g`D`Ub"

: cf'h\Y'7f]g]g'7ca a i b]\Wh]cb'D`Ubž'mci 'k]``VY'fYei]fYX'hc'UX\YfY'hc'UV\\Ydh'X']bXi ghfmdfU\\]\W

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

 $Gh\ XYbhg\ UfY\ YI\ dYWMYX\ hc\ di\ hih\ Y]f\ bUa\ Yg\ UbX\ gh\ XYbhbi\ a\ VYfg\ cb\ Yj\ YfmdU[\ Y\ cZh\ Y]f\ Ugg][\ ba\ Ybhg\ bug\ Ybhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\$

Hi fb]h]b Gi Va]gg]cb

⊋mci 'YbWci bhYf'U'dfcV'Ya 'k \Yb'UhhYa dhjb['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]hjbž'd'YUgY hY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-' ,) '' ' '%cf'Ya U]'hXYa 'cb'<u>Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui</u> ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wr`]b`UggYggUV`Y`k cf_ž`VY`]h'U`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž`U \WUgg`hYghž`U``UVcfUhcfmhYghž`U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa 'cZUggYgga Ybh'

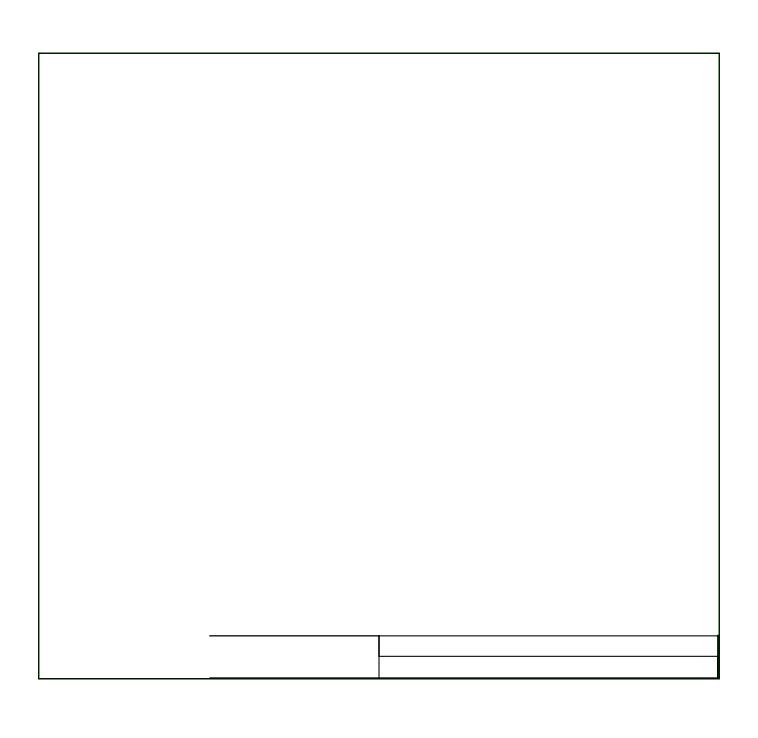
5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i\in\WbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiW\YUh]b[ihciUVW]XYbhU`mWcdm]b[iZfca iUigci fWlik]h\ci hiUW_bck iYX[Ya Ybh'i

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.$

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`h\I hcf']XYU'k]h\ci hUW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U'gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]hY[cf]Yg.

- VYMYfa UbU[Ymcifh]a Y
- i bXYfgHUbX mci f'f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'UhI BGK
 VY`Uk UfY`cZd`U[]Uf]ga žWcdmf][\hz`I BGK 'Gh XYbh'7 cXY`cZ7 cbXi Wh'UbX`5VWWdhUV`Y`I gY`cZ IBGK '=7 H'F Ygci fWYg'Dc`]Wm



FYgci fWfg

DfYgWf]VYX F Ygci fWYg

 $\bullet \text{ K YVg]hY'} - \text{`F Ygci fVWg'k]```VY'Uj U]`UV`Y'cb'h\Y'7ci fgY'A ccX`Y'k YVg]hY''$

FYWca a YbXYX FYgci fWYg

: i fh\Yf'FYUX]b[

7 cca Vgž'K "H"/ '< c``UXUmž'G">"`f9 Xg"łż'&\$\$%ž'F ZW: S` VTaa] aX5 d[e[e 5 a _ g` [USf[a` žYX]hYX'Vm'A U`XYbž A 5. '6`UW_k Y``

; U``ck Umž7"/ ?k UbUg\!5]Xccž?"ž&\$\$-žBgT1[U DWSf[a` e ;eegWe S` V 5d[e[e ? S` SYW

<agd S^aXBgT (U D WSf[a`e D WeWSdJZ

BgT (UDWSf[a`eDWh[W

ł 'H\]gʻ]gʻU``]ghcZgi dd`Ya YbhUfmfYUX]b['fYgci fWYgžk\]W\ 'a UmVY`\Y`dZ``]b`Xc]b['Z fh\Yf`fYgYUfW\"'Mci UfYžcZWci fgYžYbWci fU[YX`hc`a cj Y`VYmcbX`h\YgY`gi [[YghYX`hYI hg"

7ci fgY 9j U'i Uh]cb UbX 8Yj Y'cda Ybh

Mci f'ZYYXVUW_'[Uh\YfYX'Zfca 'h\Y'gi fj Ymg'Uhh\Y'YbX'cZh\Y'gYgg]cb'cZZYfg'j U`i UV`Y`]bdi h''Mci f Yl dYf]YbWrg'UbX'gi [[Ygh]cbg'UfY']a dcfhUbhz'UbX'h\YfY']g'U`k Umg'fcca 'Zcf']a dfcj Ya Ybh']b'hYfa g'cZ WcbhYbh'UbX'hYUW\]b['ghfUhY[]Yg'''

⇒a U[Y'7fYX]h

H\Y'Wcj Yf']a U[Y'i gYX'k]h\'h\]g'7 ci fgY'Ci h]bY'\Ug'VYYb'cVhU]bYX'Zfca 'Ub'Ubcbma ci g'cb`]bY'gci fW'"

7F = 7CG

7F = 7CG Dfcj]XYf 7cXY. \$\$\$-,;