

ARTS1120

9|dYf]YbW]b["H\YUlfY

HYfa 'C bY''##'&\$&%

7ci fgY'Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWJhjcb	D\cbY
>cbUt\Ub'6c``Yb	G	Hi YgXUmgž %\$Ua!%&da/ch\Yf hjaYg'YaU]`Zcf Uddc]bhaYbh	K YVghYf`&(*8	Ž*%'&'-',) \$+%

GWXcc~7cbhJWh~abZcfa Uhlcb

GWXcc`cZh\Y'5fhg'UbX'AYX]U

Fcca " %&ž@YjY`" žFcVYfhK YVghYf'6i]X]b['f) %(Ł

D\cbY.'f\$&Ł'-',)'(,)*

9a U]`.'gUa 4 i bgk "YXi "Ui

K YVg]hY. k k k "Ufhg"i bgk "YXi "Ui #gUa

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck``YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubgž h\Y'6YXY[U'`fPYbg]b[tcb'WJadigŁZ'; UX][U'`fP]tmUbX'5fthZ''8Yg][b'7UadigYgŁUbX't\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cfWY'5WJXYam]b'7UbVYffUŁ'cZh\Y'`UbXg'k\YfY'YUW\'WJadig'cZIBGK']g`cWJhYX''$

7ci fgY 8YW] g

7 fYX]hDc]bhg***

Gi a a UfmcZh\Y 7ci fgY

8 c mci 'k Ubhhc 'gYY'dYfZcfa UbW' `]j Y'cb 'gHJ[Y3'8 c mci 'k Ubhhc ']bX'ci h\ck ']hg'a UXY3'A UmVY'mci 'j Y VYYb'a cj YX'VmUb'UWcf'g'dYfZcfa UbW'žUa UnYX'Vmh\Y'VYUi hmcZUb']a U[Y'cf'WJi [\hU'[`]a dgY'cZ gca Yh\]b['VYmcbX'k cfXg"' =b'h\]g'Wci fgY'mci 'k]``YI d`cfY'\ck 'Ufh]ghg'WfYUhY'a YUb]b[Z ``YI dYf]YbW'g']b dYfZcfa UbW'''GHJ[]b['gWf]dhgžXYg][b]b['gWfbYgžXYj]g]b['UWf]cbg'-'mci '```YUfb'UVci hh\Y'dfcWfgcZ a U_]b['h\YUhfY'UbX'\ck 'hc'di hmci f'ck b']XYUg']bhc'dfUWf]W'''H\]g']g'U'Zci bXUhjcbU'`Wci fgY']b'dYfZcfa UbW UbX'dfcXi Wf]cb"'=icdYbg'i d'cddcfhi b]hJYg'Zcf'UWf]b[žX]fYWf]b['UbX'XYg][bžVUW_gHJ[Y'dfcXi Wf]cbž'gWf]dh k f]hJb['UbX'fYj]Yk]b['h\Y'Ufhg''

7 ci fgY @YUfb]b[Ci hWca Yg

 $\%'' 8 YgW'']VY'UbX']bhYfdfYhU'h\YUlfY'Yj Ybh]b'hYfa g'cZ]hg'a i `h]d`Y'g][b]Zm]b['Y`Ya Ybhg'UbX'h\Y]f$

5ggYgga Ybh

GYY Wci fgY a ccX Y Zcf Hug_]bglfi Wjcbg UbX UggYgga YbhWf]hYf]U"

5ggYgga YbhHUg_g

5ggYgga Ybh'hUg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX
DYfZcfa UbWY 5bU`mg]g	&\$I	% #\$' #&\$&%`%%) - `DA	%ž [:] &ž [:])
9ggUmi	(\$1	\$%#\$(#&\$&%`%%) - `DA	&ž [.] ' ž [.])
DfUWjWU``DfcYWi	' \$1	&\$#\$(#&\$&%`\$&.\$\$`DA	(ž)
±oX]j]Xi U``7 cblf]Vi lijcb'hc DfUWjWU``DfcYWi	%\$ı	&%#\$(#&\$&%`%%) - `DA	(Ž)

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% DYfZcfa UbW 5bUmg]g

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. %\\$\$\$ k cfXg

8 YHJ]`g.

 $\label{eq:continuity} FiVf]W]bX]WUf]b[``YjY``cZdYfZcfaUbW'`U[U]bghYUW``UggYggaYbhWf]hYf]Už'kf]hHYb``ZcfaUh]jY``ZYYXVUW_Z`UbXdYfWbhU[Y`[fUXY"]$

5ggYgga Ybh'& '9ggUm

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h. &ž\$\$\$ k cfXg

8YW]`q.

K f]hY cbY &z\$\$\$!k cfX 9ggUmcb U hcd]WgdYWZYX Vmh\Y 7 cbj YbYf"

 $\label{eq:continuity} FiVf]W]bX]WU]bX[Wu$

Hi fb]h]b^gYhh]b[Yh\$

	5ggYgga Ybh	9ggUmiXi YžiH\i fgXUmži%'5df]``&\$&%
K YY_', .') '5df]`!'- '5df]`	@YWhifY	DfUWMWYDfcYWn-FY\YUfgU`g"FYj]Yk fYgYUfW\" 6Y[]b`fY\YUfg]b[`]b`mcif'U``cWUhYX'jYbiY"
	Hi hcf]U`	DfuWjWU`DfcYWn-WcbhbiYfY\YUfg]b["DfYgYbhUbUWjcb`]ghUbXXYg][b'WcbWdhhcmcifHihcf/AUf_A]hWXY`"
K YY_''‰'5df]`'!'%* 5df]`	@YWn fY	DfuWjWu`DfcYWi-FY\YUfgU`g"7cbljbiYfY\YUfg]b[]b'mcif'U`cWUlYX'jYbiY"GHU[Y'U'dfcj]g]cbU`kU`_!h\fci[\`cZh\Y'dYfZcfaUbW'f]hg'gYeiYbW'gžUffUb[YaYbhg'UbX'YZZYWgŁ"
	Hi lcf]U`	DfuWjWu`DfcYWi-WebljbiYfY\YUfg]b[": i``fY\YUfgU`cZWeadYHYdYfZefaUbWY-dfYgYbhmeifgeibX#][\ljb[#YW\d`Ub'he'meif'hihef'UbX'AUf_A]hVXY``"
K YY_'%\$.'%-'5df]`'!'&' 5df]`	@YWn fY	DfUW]WU`DfcYWi—'Hi YgXUm&\$'5df]` &\$&%"'HYW\#XfYgg'fY\YUfgU`ž' \$'a]bi hYg'dYf'[fci dž VYhk YYb'\$\$Ua 'UbX'%"\$\$da ž'h]a Yg'hc'VY

FYgci fW/g

DfYgWf]VYX F Ygci fWyg

91 dYWYX fYgci fWg Zcf'h\Y Wci fgY UfY Uj U] UV Y Zfca 'I BGK @JVfUfmj]U A ccX Y "'

Ghi XYbhgʻUfYʻYl dYWhYXʻhcʻUhhYbXʻhk cʻdYfZcfa UbWYgžʻcbYʻcbʻWUa di gžʻcbYʻcZZWUa di gžʻUgʻdUfhcZh\Y Wci fgY"'8YhU]ʻgʻUVci hdYfZcfa UbWYgʻUfYʻdfcj]XYXʻcbʻA ccX`Y"

FYWca a YbXYX FYgci fWYg

7 ci fgY '9j U'i Uh]cb 'UbX '8 Yj Y`cda Ybh

K Y`k Y`Wca Y`Wcbghfi Whj Y`ZYYXVUW_`—'YgdYWjU``mik f]hh/b`ZYYXVUW_`fl/a U]`gž'bch/g`YhW'L`cb`h\Y`Wci fgY`Wcbh/bhzghfi Whi fY`UbX`UggYgga Ybha Yh\cXg`—'bchcb`mUhh\Y`WcbWi g]cb`cZh\Y`Wci fgYžVi hU`gc`Ug`k Y`[cU`cb["'5hh\Y`YbX`cZh\Y`Wci fgY`k Y`k]```]bj]h/`mci 'hc`dfcj]XY`ZYYXVUW_`i g]b[`I BGK fig`Wci fgY`Yl dYf]YbW/gi fj Ym'

A UbmUgdYWg`cZh\]g`Wci fgY`UfY`h\Y`fYgi `hcZ]bbcj Uhjj Y`gh XYbhZYYXVUW_`Zfca `dfYj]ci g`mYUfg`-

Gi Va]gg]cb cZ5ggYgga YbhHUg_g Hi fb]h]b Gi Va]gg]cb

⊋mci 'YbWci bhYf'U'dfcV`Ya 'k \Yb'UhhYa dh]b['hc'gi Va]h'mci f'Ugg][ba Ybh'h\fci [\'Hi fb]h]bž'd`YUgY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

• i bXYfgHJbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbh'Uhil BGK

5 WUXYa]W±bZcfa Uhjcb