

# **ARTS2091**

AcV]`Y'7i `h fYg

HYfa "Hk c" ## "&\$&\$

# 7ci fgY<sup>-</sup>Cj Yfj ]Yk

### GHJZZ7cbHJWh8YHJ]`g

#### 7 cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`]lm	@cWJhjcb	D∖cbY
A ]WXY`Y`NUddUj ][ bU	a "nUddUj ][ bU4 i bgk "YXi "Ui	VmUddc]bha Ybh	KYVghYf" WF	

### GWXcc`7cbHJWh = bZcfa Uh]cb

 $GVXcc``cZh\Y`5fhg`UbX`AYX]U$ 

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D\cbY. f\$&Ł'-',) '(,) \*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. k k k "Ufhg"i bgk "YXi "Ui #gUa

 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg`UbX`AYX]U'kci`X``]_Y'hc'FYgdYWM\ ``m'5\\_bck`YX[Y'h\Y'HfUX]h]cbU``7i\ghcX]Ubgžh\Y'6YXY[U``fPYbg]b[hcb'\WJa\ di\głž';\UX][\U``fP\]hm\UbX'5fh\/ '8Yg][\b'7\Ua\ di\gYgŁ'\UbX'h\Y'B[i\bb\Uk\U`\d'\cd'\%\]$ 

# 7ci fgY 8YHJ] g

7 fYX]hDc]bhg\*\*

Gi a a UfmcZh\Y 7ci fgY

H\]gigi VYWik ]```gi fj Ymih\Y`\]ghcfmcZa cV]`Y`UbXidcfhUV`Y`a YX]U`Zfca `hfUbg]ghcfifUX]cg'h\fci [\`hc]D\cbYg'k]h\]b`U``Uf[Yf'WcbhYl hcZa cV]`Y`W``hi fYg']b`k\]W\`k Y`a cj Y`Zfca žij ]``U[Y`hc`W]mž`\ca Y``]ZY`hc`WUfW``hi fYž'Zfca `U]fdcfhhc`]bhYfbYh''Ghi XYbhg'k]```VY`UV`Y`hc`]bj Ygh][UhY`h\Y`W`ffYbhghUhY`cZd`Um]b`h\Y`a cV]`Y

# 5ggYgga Ybh

### 5ggYgga Ybh'HUg\_g'

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Hi hcf]U``HUg_g`	&\$I	&-#\$*#&\$&\$`%%) - `DA	%ž&Ž Ž(
G\cfh9ggUm	) \$1	% #\$+#&\$&\$`%%) - `DA	%ž&ž(
HU_Y!\ca Y'Yl Ua '	' \$1	&, #\$+#&\$&\$`\$\$\$`5A	%ž&Ž Ž(

#### 5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% Hi hcf]U`HUg\_g

GhUfhXUhY. K YY\_"%"h hcf]U"

8 YW] g.

 $\label{thm:condition} Hi \ hcf]U``HUg\_g`Wca V]b]b[ \ 'a \ i \ 'h]d`Y`Wkc]WY`UbX`g\cfhUbgk Yf`fYgdcbgYg`Yei ]j \ U`Ybh'hc', $$!%$$$'k cfXg`]b \ hcfU`"$ 

Gh XYbhg k ]``fYV\]j Y fi Vf]W[fUXY"

#### 5XX]h]cbU`XYhU]`g.

5ggYgga Ybh& G\cfh9ggUm

GhUfhXUhY. Bch5dd`]WUV`Y

8YHJ]`q.

%) \$\$! &\$\$\$ k cfXg" Ghi XYbhg k ]``fYVW]j Y fi Vf]WUbX Wca a Ybhg"

Hi fb]h]b gYh]b[. H\]g Ugg][ ba Ybh]g gi Va ]hhYX h\fci [\ Hi fb]h]b UbX gh XYbhg Xc bchgYY Hi fb]h]b g]a ] Uf]hmfYdcfhg"

5ggYgga Ybh' . HU\_Y!\ca Y YI Ua

GhUfhiXUhY. '&+#\$+#&\$&\$ '\$-.\$\$ '5A

8YHJ]`q.

HU\_Y!\ca Y`YI Ua `Wcbg]gh]b[ `cZ' `g\cfhUbgk Yf`ei Ygh]cbg`fYei ]f]b[ `W" \$\$`k cfX`Ubgk Yfg"`Mci `\Uj Y`&(

\ci fg'hc'gi Va ]hmci f'Ubgk Yfg'Zfca 'h\Y'gHJfh'XUhY'UbX'hJa Y"

 $\label{thm:condition} \mbox{Hi fb]h]b"gYh]b" Low Ybh"]g"gi Va ]hhYX"h\fci [\h]b" UbX"ghi XYbhg"Xc"bch"gYY"Hi fb]h]b g]a ]`Uf]hmfYdcfhg" \mbox{Hi fb]h]b"UbX"ghi XYbhg"Xc"bch"gYY"Hi fb]h]b g]a ]`Uf]hmfYdcfhg" \mbox{Hi fb]h]b"UbX"ghi XYbhg"Xc"bch"gYY"Hi fb]h]b g]a [\h]b"UbX"ghi XYbhg"Xc"bch"gYY"Hi fb]h]b g]a [\h]b g]a [\h]b g[\h]b g[\h]$ 

# FYgci fWyg

#### DfYgWf]VYX F Ygci fWYg

 $HY'HYI'Wcc_'Zcf'HX]g'Wci'fgY']g.$ 

NUddUj ][ bUž'A "'f&\$%&Ł"'<u>8 ]aWci fgY'cZHk ]hhYf'UbX'GcWU''A YX]U</u>ž@cbXcbž'7cbh]bi i a "

 $\#i]g'Uj\ U]'UV'Y'Ug'Ub'Y!Vcc\_'j\ ]U'h\Y'`]VfUfmcf'Ug'U'df]bh'Vcc\_']b'h\Y'I\ BGK\ 'Vcc\_g\cd''$ 

#### FYWca a YbXYX FYgci fW/g

FYWca a YbXYX'fYgci fWrg'k]```VY']bWi XYX']b'h\Y'fYUX]b[``]gh'cb'A ccX'Y'j]U'@Y[Ubhc"

#### 7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

: YYXVUW\_'Zcf'h\]g'Wci fgY`k]``'VY`[ Uh\YfYX'Vch\`]bZcfa U``mž']b'hi hcf]U`gž'UbX'Zcfa U``mžj ]U'h\Y'a m9l dYf]YbWk gi fj YmbYUf'h\Y'YbX'cZgYa YghYf"

#DidfYj ]ci gimYUfgighi XYbhgi\Uj YiUg\_YXiZcfiVYbXYXiYUfb]b[ik]h\inyWhi fYgiXYi]j YfYXicbi]bY"=\Uj Y
fYgdcbXYXihcih\]giZYYXVUW\_VmcZYf]b[icbi]bYiYWhi fYg":H\YiYWhi fYik]ivVYiXYi]j YfYXiUgig\cfhij]XYcgž
Uicb[ik]h\ich\YfifYgci fWrgigi W\iUgia i h]a YX]Užei]nnYgifhcia U\_Yigi fYimci ii bXYfghUbXih\Yia UhYf]Uiug
k Yia cj Yih\fci [\ih\YiWci fgYtžiUbXi]b\_qihciYI Ua diYgicZa cV]Yia YX]Uii gY"

# Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

# Hi fb]h]b Gi Va ]gg]cb

Image: Ybwci bhYf'U'dfcV'Ya k \Yb'UhYa dhjb['hc'gi Va ]hmci f'Ugg][ ba Ybhh\fci [\'Hi fb]h]bz'd'YUgY

HY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-', ) "''' %cf'Ya U]''h\Ya 'cb'Y! hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui ""Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft'''=\mathred{Image: Wa Jhmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\'Hi fb]h]b'mci 'a UmUdd'm\mathred{Image: Wa Jhmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\'Hi fb]h]b'mci 'a UmUdd'm\mathred{Image: Wa Jhmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\'Hi fb]h]b'mci 'a UmUdd'm\mathred{Image: Wa Jhmci f'Ub'Y! hYbg]cb\mathred{Image: Wa Jhmci h\Yf'f'Y'j UbhXcW a Ybhg\mathred{Image: Wa Uj''9! hYfbU''Gi ddcfhmci 'k ]'`

JbWi XY'Ug'Yj ]XYbW' hc'gi ddcfhmci f'Y! hYbg]cb'Udd']\wUh]cb"'\mathred{Image: Wa Uj''9! hYfbU''Gi ddcfhmci 'k ]'`

Ui hca Uh]\wU'`mfYW']j Y'U'h]\w\_Yhbi a VYf\mathred{Image: hY'Yd\cbY'mci 'k ]\tag{Y}\wu''mug\_'\mathred{Image: Wa'\mathred{Image: hY}\wu''mug\_'\mathred{Image: hY}\wu''mug\_'\mathred{Image: hY}\wu''mug\_'\mathred{Image: hY'Yd\cbY''mci 'k ]\tag{Y}\wu''mug\_'\mathred{Image: hY'\mathred{Image: hY'\mathred{I

; YbYfU``mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\W)``mij ]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\U`hYfbUhjj Y'gi Va ]gg]cb'XYHJ]`g''

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# 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU\_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga ]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY