

# **IEST7600**

=bX][Ybcig?bck`YX[Y`DUfhbYfg\]dg`]b`7cbgYfjUh]cb7 7Uf]b[`Zcf`7cibhfm

HYfa 'Hk c''#'&\$&%

## 7cifgY<sup>·</sup>8YHJ]`g

## 7 fYX]hDc]bhg\*\*\*

## Gi a a UfmcZh\Y'7ci fgY

•••X][Ybci g'\_bck YX[Y'\c`XYfg'UfY'k cf\_]b['k]h`\ck 'hc`Uff]W`UHY'hY]f`\_bck YX[Y'dfUWf]Wfg'UbX'VY`]YZg'hc
bcb! •••X][Ybci g'UbX'bcb!`cWU``Ui X]YbWfg'' •• h\g'Wci fgYžmci 'k]``ZcW g'cb'Yh]WU``UbX'Yei ]HUYY'k Umg'cZ
]bhY[fUh]b[' •••X][Ybci g'UbX``cWU``\_bck `YX[Y'gmghYa g'k]h\ K YghYfb'gW]Ybh]Z]W\_bck `YX[Y'gmghYa g'hc
]bZcfa 'gi gHU]bUV]`]miUbX'WcbgYfj Uh]cb'dc`]WnUbX'dfUWf]Wf'''Nci 'k]```YUfb'UVci hUddfcdf]UhY'UbX'YZYWf] Y
k Umg'hc'g\UfY'UbX'Wca V]bY'h\YgY'\_bck `YX[Y'gmghYa g'Zcf'Wc``UVcfUh] Y'Ybj ]fcba YbHU``YUXYfg\]d"' •• hY
a ]XghcZ[`cVU``Wf]gYgž]bWi X]b['W]a UhY'X]gfi dh]cbž``Uf[Y'gWUY'YI h]bWf]cbgžUbX'YI UWFfVUhYX'Vi g\ZfYgž
mci 'k]```fYh\]b\_'k Umg'gcW]YhmWUb'WcbWYdhi U`]gY'Ybj ]fcba YbHU``dfcV'Ya g'UbX'WcbgYfj Uh]cb'dfUWf]Wfg''' •
UXX]h]cbž'mci 'k]```]bj Ygh][UhY'\ck 'hc'Vi]'XfY[]cbU'žbUh]cbU'ž'UbX'[`cVU``gW]YbWf'dc`]Wnh\Uh]g']bWi g]j Y'cZ
g]hi UhYX' •bX][Ybci g'UbX``cWU``\_bck `YX[Y'gmghYa g'k]h\ci hWca dfca ]g]b['h\Y']bhY[f]micf``Y[]h]a UWncZ
gW]Ybh]Z]Wž •bX][Ybci gźcf``cWU``\_bck `YX[Y'gmghYa g'k]h\ci hWca dfca ]g]b['h\Y']bhY[f]micf``Y[]h]a UWncZ
gW]Ybh]Z]Wž •bX][Ybci gźcf``cWU``\_bck `YX[Y'gmghYa g''

### 7cifgY`@YUfb]b[`CihWcaYg

%" 8YgWf]VY h\Y ]bh/fWcbbYWh/XbYgg cZW h fY UbX YWc c[m]b = bX][Ybci g UbX cWU \_\_bck YX[Y gmgh/a g UbX h Y dcgg]V]]h]Yg Zcf Yh ]WU ]bh/[fUh]cb k ]h K Ygh/fb gW]Ybh]Z]W\_bck YX[Y &" 5dd ma i h]d Y Yj ]XYbW YUgYg hc h Y h Ycfm UbX dfUW]W cZ UbX fYghcfUh]cb UbX WUfY

## 5ggYgga Ybh

< Ufj UfX fYZyfYbWjb[ 'gmghYa 'g\ci `X'VY'i gYX'Zcf'YggUmUbX'ZjbU``fYZYWjcb"</li>

5 "UggYgga Ybhg k ]" VY ci h]bYX ]b WUgg ]b k YY\_ %

## 5ggYgga YbhHUg\_g

5ggYgga YbhHJg_	K Y][ \h	8iY`8UHY	GhiXYbhi@YUfb]b[ CihWcaYgʻ5ggYggYX
DYfgcbU``@YUfb]b[ `>ci fbU``	&\$1	Źſghŕči fbU``Xi Y`k YY_`% \$(#\$*#&\$&%&da `h\Yb k YY_`mžk ]h\`h\Y`ŹbU``ći fbU` Xi Y`k YY_`*`\$-#\$+#&\$&%&da	%ž' ž(
9ggUmi	' \$I	% #\$+#&\$&%`%%\$\$`DA	%ž`'
FYZYW9jcb	)\$1	: ]bU``k f]thYb`fYZYWf]cb`Xi Y : f]XUmcZk YY_`%\$`fБi [igh *Ł	%ž`&ž'' Ž'(

## 5ggYgga Ybh8YhJ]`g

5ggYgga Ybh% DYfgcbU`@YUfb]b[ '>ci fbU`

GHJfhXUHY.Bch5dd`]WUV`Y

@Yb[h\.'a]b]aia'&\$\$`kcfXg`UbX`aUI]aia')\$\$`kcfXg`Zcf`YUW\`cZkYY\_g`%\*

#### 8 YHJ]`g.

H\Y`ĉi fbU``k]``VY`\_YdhH\fci [\ci hH\Y`HYfa žk]H\`kYY\_`mYbHf]Yg`fgi Va]HHX`kYY\_`m—`ZYYXVUW\_`j]U`jYfVU` cf`kf]HHYb`Wca a YbhgŁ"`FYei]fYg`Wf]h]WU``UbX`dYfgcbU``Yb[U[YaYbhk]H\`Wci fgY`WcbHYbhUbX`YI dYf]Ybh]U` `YUfb]b[ž'UbX`a Umi]bWi XY`g\cfhfYZYWf]cbg`cb`U`bi a VYf`cZdfY!gYhei YgH]cbg"`@Yb[H\.`&\$\$`k cfXg`dYf kYY\_`Zcf`kYY\_g`%I\*"

: YYXVUW\_j ]U'U'fi Vf]Wzbi a Yf]WU`a Uf\_z'UbX'Wca a Ybhg"

#### 5XX]h]cbU``XYhJ]`g.

H\Y`cifbU``HJg\_'Zcf`kYY\_'%k]``VY`dcgHYX`cb`accX`Y`VYZcfY`HYfa`gHJfhg`UbX`]g`hc`VY`Wcad`YHYX`Zcf X]gWigg]cb`]b`WUgg`cb`:f]XUmcZkYY\_`%

>ci fbU`g`Zcf`gi VgYei Ybhk YY\_g`k ]``VY`VUgYX`cb`mci f`ck b``YUfb]b[`fYZYWf]cbg`fWf]hYf]U`UbX`[i]XUbWY dfcj]XYX`]b`WUgg`k YY\_`%±ž`i b`Ygg`ch\Yf`gdYW]Z]WhUg\_g`UfY`gYh'

Gi Va ]gg]cb bchYg. Gi Va ]hth fci [ \ a ccX`Y``]b\_`cb`: f]XUmZcf`YUVX`cZk YY\_g`%'\*"

Hi fb]h]b`gYH]b[.`H\]g`]g`bchU`Hi fb]h]b`Ugg][ ba Ybh

5ggYgga Ybh'& '9ggUm

@Yb[h\.\*&\$\$!%(\$\$`kcfXg`fbch`]bWi X]b[`fYZYfYbW\*``]ghL

#### 8YHJ]`g.

H\Y'YggUmfUVci h%2&\$\$`k cfXgŁ'k]```ci h]bY'Yh\]WU``UbX'Yei ]hUV'Y'k Umg'cZ]bhY[fUh]b[`+aX][Ybci g'UbX'`cWU` \_bck `YX[Y'gmghYa g'k]h\'K YghYfb'gW]Ybh]Z]W\_bck `YX[Y'hc']bZcfa 'gi ghU]bUV]`]miUbX'WcbgYfj Uh]cb'dc`]Wn UbX'dfUW]WY''`@YUfb]b['k]``VY'VUgYX'cb'gYa]bUfg'UbX'dfYgYbhUh]cbgž'fYUX]b[gž'UbX'Wcbj YfgUh]cbg''Gca Y \ifX'Y'Ugg][ba Ybhg'gi W\'Ug'cb`]bY'ei]nnYgž'k]``VY']bWi XYX''

: YYXVUW\_`k]```VY`[]jYb`]b`h\Y`Zcfa`cZU`fiVf]Wf]bWiX]b[`h\Y`\ifX`Y`hUg\_głžibiaYf]WU``aUf\_žUbX WcaaYbhg"

#### 5XX]h]cbU``XYHJ]`g.

<i fX`Y`Ugg][ ba Ybhg`k ]```VY`gYhZcf`k YY\_g`&! (`UbX`dfcj ]XYX`cb`a ccX`Y"

9ggUmWf]hYf]U'UbX'[i]XUbWY'k]``VY'dfcj]XYX']b'WUgg']b'kYY\_'%fbiVa]gg]cb'XUhY'Zcf'YggUmi]g'>i `m'% Ł"

Gi Va ]gg]cb bchYg. 'Gi Va ]hh\fci [ \ 'a ccX`Y``]b\_

Hi fb]h]b`gYh]b[.`H\]g`]g`bchU`Hi fb]h]b`Ugg][ ba Ybh

5ggYgga Ybh' . FYZYWjcb

GHJfhXUHY.Bch5dd`]WUV`Y

@Yb[h\.`&\$\$\$`k cfXg`fbch`]bWi X]b[`fYZYfYbW``]gHz

#### 8YHJ]`g.

H\Y`ZJbU``UggYgga YbhfUVci h&\$\$\$`k cfXgŁ'k]``VY`U`fYZYWJcb`cb`k \Uh\Ug`VYYb``YUfbhž'fYZfUa YX`UbX i bXYfghccX`Xi f]b[`'h\Y`Wci fgY"`H\Y`UggYgga Ybhk]```]bWi XY`U`k f]hYb`HUg\_`fUggYggYX`Vmi b]j Yfg]hm UWUXYa ]WgŁ'UbX`h\Y`ch\Yf`Wca dcbYbhg`cZh\Y`UggYgga Ybhk]```VY`VUgYX`cb`XYa cbghfUh]cb`cZ i bXYfghUbX]b[``]b`h\Y`Z]Y`X"`H\Y``cWU``\_bck`YX[Y`Ui h\cf]h]Yg`k \c`\cghih\Y`Z]Y`X`Hf]d`k]```Wc!XYg][b`h\]g UgdYWicZh\Y``YUfb]b[``HUg\_`UbX`VY`Wc!UggYggcfg`cZWca dYHYbWY#YUfb]b[`ci hVca Yg"

: YYXVUW\_'j ]U'U'fi Vf]Wž'bi a Yf]WU`'a Uf\_ž'UbX'Wca a Ybhg"

#### 5XX]h]cbU``XYHJ]`g.

$$\label{eq:hyperbolic} \begin{split} H\Y`HJg\_XYg][\ bYX`UbX`UggYggYX`VmHfUX]h]cbU``7 i ghcX]Ubg`k ]``VY`i bXYfHJ_Yb`Xi f]b[``H\Y`a i `h]!XUmZ]Y`X ff]d`UbX`k ]``VY`k cfh`&) i ``f\U`ZcZh`Y`) $i & & \\ \end{split}$$

H\Y`ZJbU``kf]hYb`fYZYWJcb`faUf\_YX`VmWcifgY`WcbjYbcfgŁk]```VY`cih]bYX`Xif]b[`WUgg`]b`kYY\_`%UbX`]g XiY`YbX`cZhYfa`fIf]XUm5i[igh\*h\žkYY\_`%Ł"

Gi Va ]gg]cb bch/g. Gi Va ]hZbU`k f]hh/b fYZYWjcb h fci [ \ ``]b\_`cb a ccX`Y"

Hi fb]h]b`gYh]b[.`H\]g`]g`bchU`Hi fb]h]b`Ugg][ ba Ybh

Xi Y``UghXUmcZhYfa `fl f]XUm5i [i gh\*t"

## FYgci fWg

#### DfYgWf]VYX F Ygci fWyg

5 W fUHYX'gYhcZa UbXUhcfmfYgci fWg'k ]``VY'Uj U]`UV'Y'h\fci [ \`@Y[ Ubhc'UbX'cb'h\Y'Wci fgY'a ccX'Y'g]HY Zcf'h\Y'gHJfhcZhYfa "

H\YfY`]g`U`j`UghUffUmcZ`]hYfUh`fY`UbX`kYV]bUfgždcXWJghg`YhWžh\Uh]bZcfa`h\]g`Wci`fgY"`=h`]g`ghfcb[`m fYWca a YbXYX`h\Uhmci`ghUfh`cc\_]b[`UhfY`Yj`UbhfYgci`fWYg`VYZcfY`h\Y`Wci`fgY`ghUfhg"`Gca Y`fYgci`fWYg fUj`U]`UV`Y`h\fci`[`\`@Y[Ubhc`UbX`Ug`YVcc\_g`]b`I`BGK```]VfUfmŁhc`ghUfhik]h\`]bWi`XY.

"8Uf\_'9ai "'Vm6fi WY'DUgWcY'

"@cj]b['7ciblfm"'7\UdhYf"%fdd"%%'cb";i`U[U7'6]UaUb[U'fdfYdUfUh]cb"Zcf"Z]Y`X'hf]dłŁ'&\$&\$

"Gcb[`]bYg'! H\Y'Dck Yf'UbX'h\Y'Dfca ]gY" VmA Uf[c'BYU`'UbX'@mbbY'? Y``m&\$&\$'

"GUWFYX"9Wc`c[m""Vm:]f\_Yh6Yf\_Yg"&\$%&

#### FYWca a YbXYX<sup>-</sup>FYgci fWYg

5<sup>m</sup>]ghcZk]XYfffYWca a YbXYXfYgci fWfgffYVcc\_g]b1 BGK <sup>m</sup>]VfUfmUbX<sup>m</sup>]b\_YX<sup>\*</sup>hc<sup>\*</sup>@Y[UbhcŁ]bWi XYg.

"Gcb[gd]fU`g`!`g\Uf]b[`k ca Ybfg`k]gXca `cZ7 ci bhfmh\fci [\`gcb[`]bYg"`Vmh\Y`; UmfK i `; fci d`cZK ca Ybž &\$% ž5``Yb'/`I bk]b

"H\Y'8fYUa]b[ 'UbX'ch\Yf'YggUmg"'VmK "9"<"'GHUbbYf'

"6fU]X]b[ 'Gk YYh[ fUgg'! '€X][ Ybci g'K ]gXca žGW]Ybh]Z]W? bck `YX[ Y'UbX'h\Y'HYUW\]b[ g'cZD`Ubhg"`VmF cV]b K U``? ]a a YfYf'&\$% '! 'fYUX'd&( %&) ' "

Hk c'df]bhVcc\_g'Uj U]`UV`Y`]b'I BGK ``]VfUfm`"GUbX'HU`\_"`VmHmgcb'M b\_UdcffU

#### 7 ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

H\]g`]g`h\Y`]bUi [ i fU``mYUf`Zcf`h\]g`Wci fgY"`5g`k Y```Ug`h\Y`a m9I dYf]YbWY`ZYYXVUW\_žU`gi fj Ymik ]```VY dfcj ]XYX`hc`ghi XYbhg`hc`Wca d`YhY`Zcf`ZYYXVUW\_`cb`h\Y`ZY`X`hf]dg"

## Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

## Hi fb]h]b Gi Va ]gg]cb

Zmci YbWci bhYf'U'dfcV'Ya 'k \Yb'UhYa dhjb[ 'kc'gi Va ]hmci f'Ugg][ ba Ybhih fci [ \ 'Hi fb]hjbž'd'YUgY hY'Yd\cbY'9I hYfbU'`Gi ddcfhcb'-', ) '' ' %cf'Ya U]`'h Ya 'cb'YI hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh \ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ''Zmci UfY'i bUV'Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZUi 'hk ]h 'Hi fb]hjb'mci 'a UmUdd`mZcf'Ub'YI hYbg]cbžVi hmci a i ghfYhU]b'mci f'hjW\_Yhbi a VYf'Zfca '9I hYfbU'`Gi ddcfhfU'cb[ 'k ]h 'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc ]bWi XY'Ug'Yj ]XYbWY'hc'gi ddcfhimci f'YI hYbg]cb'Udd`]WUhjcb'''Zmci 'Ya U]`'9I hYfbU'`Gi ddcfhimci 'k ]`

## 5WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

D`U[]Uf]ga `]g`i g]b[`h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b[`h\Ya `Ug`mci f`ck b"`=h`WUb`hU\_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b[`hc`UVW]XYbhU``mWcdm]b[`Zfca `U`gci fWY`k]h\ci hUW\_bck `YX[Ya Ybh'

- i bXYfgHJbX\*mci f\*f][\hg\*UbX\*fYgdcbg]V]`]h]Yg\*Ug\*U\*ghi XYbh\*Uhil BGK
- VY 'Uk UfY 'cZd'U[]Uf]ga ž Wcdmf][ \hzi I BGK 'Ghi XYbhi7 cXY 'cZ7 cbXi WhubX '5 WW dhuV Y I gY 'cZ I BGK '=7 H F Ygci fW g'Dc']Wh
- VY Uk UfY cZh Y gHUbXUfXg cZVY Uj ]ci f YI dYWHYX cZYj YfmcbY ]b h Y I BGK Wea a i b]m
- `cWUHY'gYfj ]WYg'UbX']bZcfa UHjcb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``'h\Y fY`UhYX'UgdYWfg'cZ9@=G9'k]``\Y`d'mci 'a U\_Y'h\Y'a cghcZmci f`gh X]Yg'Uh'l BGK "' \htd.#gi VYWf[i]XYg"`]VfUfm'i bgk "YXi "Ui #Y`]gY#UVci hY`]gY